Online Course on Debt Sustainability Analysis (DSAX)

Part 1: Principles of Debt Sustainability

DSAx Part 1:

Principles of Debt Sustainability

Part 1 Unit 1:

Learning Objectives and Structure of Part 1

Learning Objectives of Part 1

- Learn about key concepts of debt sustainability analysis
- Inderstand the dangers of high debt
- ✓ Derive debt dynamics for different types of debt
- ✓ Discuss the role of fiscal adjustment and other macroeconomic policies

Structure of Part 1

✓ Unit 1: Overview

2

- ✓ Unit 2: Defining debt sustainability
- ✓ Unit 3: Why is debt sustainability analysis important?
- ✓ Unit 4: Public debt sustainability in a closed economy: part 1
- ✓ Unit 5: Debt dynamics Public debt sustainability in a closed economy: part

Structure of Part 1

- ✓ Unit 6 Public debt sustainability in an open economy
- Unit 7 Chipping away at public debt (Adjustment paths and their implications)
 Unit 8 Role of macroeconomic policies
 Unit 9 External debt sustainability: part 1
- ✓ Unit 10 External debt sustainability: part 2

Part 1 Unit 2:

Defining Debt Sustainability

UNIT \mathbf{M}

✓ Understand the concept of sustainability

Master the relevant terminology

✓ Identify relevant indicators of solvency and liquidity

 Familiarization with various types of DSA conducted by the IMF/World Bank OUTLINE

 Debt sustainability from different angles
 Debt burden indicators
 Introduction to IMF/World Bank Debt Sustainability Analysis (DSA)

Part 1 Unit 2: Lecture 1

What is Sustainability?

OUTLINE

✓ Debt Sustainability from Different Angles:

Academic

Pragmatic

Intertemporal Solvency Condition



Primary expenditure = Expenditure - Interest expenditure

Discounting: refers to calculating the present discounted value

Intertemporal Solvency Condition

✓ When a government, business or individual is solvent, it is able to service its current debt out of future income or surpluses. A person with a small debt and large future income is solvent.

<u>Example</u>: Consider a business with debt of \$20,000 and a prospect of annual profits of \$10,000. The business is solvent as this debt can be serviced from future profits.

Intertemporal Solvency Condition

✓ A counter-example is a Ponzi-scheme. In such schemes, initial debt is serviced by relying on new investors, rather than serviced out of future surpluses. Solvency is "very much like honesty: it can never be fully certified, and proofs are slow to materialize."

Guillermo Calvo

Academic Definition of Debt Sustainability

Debt is **sustainable** if the intertemporal solvency condition is satisfied, that is, if the expected present value of future primary balances covers the existing stock of debt.

The ability to

postpone generating primary surpluses to cover for the existing debt obligations into the future

makes solvency

a relatively weak requirement

Academic Perspective

Precise



Unobservable



Forecasting Future



Pragmatic Definition of Debt Sustainability

Debt is **sustainable** if projected debt ratios are stable or decline, while also being sufficiently low.

Debt is unsustainable if projected debt ratios increase or remain high.

Pragmatic Definition of Debt Sustainability

Pragmatism consists in recognizing that the <u>ratio of debt to capacity to</u> <u>pay</u> is what matters in order to avoid a debt crisis.

To be sustainable, debt cannot grow faster than incomes and the capacity to repay it.

Pragmatic Definition of Debt Sustainability

Another aspect of pragmatism is to recognize that economies are subject to <u>shocks</u>.

A debt ratio which is <u>declining but</u> <u>high can still be **unsustainable** if it</u> associated with a high risk of default.

Example of Pragmatic View of Sustainable Debt

Debt/GDP



Taking Solvency Condition to the Data

Solvency vs. Non-explosive Debt Ratios:

✓ Useful result when interest rates are higher than the growth rate:

if the ratio of debt to GDP is either **stable** or **declining** <u>in the long run</u>, the solvency condition is automatically met.

Risks to Sustainability

The projected trajectory and the level of debt should be based on realistic assumptions about the underlying macroeconomic variables

The resulting gross financing needs have to be evaluated

The market perception of the sovereign risks has to be factored in based on debt maturity structure, its currency composition, its creditor base, etc.

Part 1 Unit 2: Lecture 2

Define Debt Sustainability

OUTLINE

✓ Debt Sustainability from Different Angles:

Economic Policy Definition

Economic Policy Definition of Debt Sustainability

Debt is sustainable if the country (or its government) does NOT, in the future, need to default or renegotiate or restructure its debt or make implausibly large policy adjustments.



FINANCIAL TIMES

Home	Wo	World		s M	arkets	Global Economy		Lex	C	Comment	
Video	Interactive	Blogs	News feed	Alphaville	beyondbrics	Portfolio	Special F	Reports	In depth	Today's	

Search ai

Search sp

September 19, 2004 11:14 pm

Argentina nears \$100bn debt default agreement

By Adam Thomson

Argentina's battle to get bondholders to accept the largest sovereign debt reduction in the history of capitalism is almost won.

Wall Street analysts and, privately, some bondholder representatives agree that most of the country's creditors would accept a proposal to restructure about \$100bn in defaulted debt that offered recovery values of a little over 30 cents in the dollar. That is just above the price of defaulted bonds on the secondary market.

Debt Restructuring

EU Economy

Home	World	 Companies * 		Markets *		Global	Lex≚		
Economic (Calendar	Money Supply	Americas	China	EU	India	Middle East	UΚ	US

Last updated: March 8, 2012 10:22 pm

Greek debt swap support close to 95%

By Richard Milne in Oslo, Kerin Hope in Athens and Peter Spiegel in Brussels

The largest debt restructuring in history was heading for a successful outcome last night as Greece looked set to see a participation rate of close to 95 per cent for its €206bn bond exchange.

One person involved in the deal said that more than 90 per cent and possibly more than 95 per cent of investors had taken part, assuming collective action clauses (CACs) were used to bind dissenting holders of some bonds.



More video

"PSI is a success. Will it exceed 95 per cent? There is a good chance," the person said A Greek cabinet minister said: "It will be good news tonight."

The Greek government will announce the official results of its two-week campaign to win over private holders of its debt early on Friday morning. But late on Thursday night bankers and senior Greek officials briefed in the results said an overwhelming majority of investors had voted in favour of the deal, which will see them suffer MARKETS INSIGHT

March 7, 2012 9:49 pm

Greek deal will buy time but hard work lies ahead

By Richard Milne

It is as complex as it is big. Greece's €206bn debt restructuring has left people drowning in a sea of figures, struggling to make sense of the deal.

Investors will get up to 24 new securities for each existing bond, a 66 per cent threshold for use of so-called "collective action clauses" but a 50 per cent quorum, and a participation rate that needs to be 95 per cent – or is it 90 or 70 per cent instead? Confused?

ڬ 🖪 👫 in

More

ON THIS STORY

Greece inches closer to €206bn debt deal

Bondholders in stand-off with Athens

Investors help Athens over bailout hurdle

The Short View Greece ditto Argentina

Video No PSI for Portugal

MARKETS INSIGHT

Prompt action required on eurozone deflation

Debt crisis has left Germany vulnerable

Curse of euro lands ECB in tricky dilemma EM bonds in better shape after

sell-off

The simple fact is that, for all its complexity, Greece has structured this deal so that it is likely to be reasonably successful. Retroactively inserting collective action clauses, which allow the decision of a majority of bondholders to bind all investors, may seem unfair to holdouts. But it all but ensures that Greece will be able to get all its Greek law bondholders to take part, giving it about 86 per cent participation.

The question will then be to see how many international law bonds, which account for the other 14 per cent of the €206bn, are tendered in the exchange. It is unlikely enough will be tendered to reach the 95 per cent the International Monetary Fund has said is necessary to get Greece's debt down to 120 per cent of gross domestic product by 2020.

Greece has threatened not to pay any international law holdouts at all. That would open the way for a legal battle. But it also raises the prospect that Athens could raise more money than expected by simply not paying some bondholders.

Policy Adjustments

Last updated: November 8, 2012 10:09 am

Athens narrowly passes austerity bill

By Kerin Hope in Athens



The Greek parliament narrowly approved a fresh austerity package on Wednesday night, opening the way for international lenders to transfer a long-delayed €31.5bn slice of funding and take steps to ease the terms of the country's €174bn bailout.

Lawmakers ba FINANCIAL TIMES

August 9, 2013 2:54 pm

By Kerin Hope in Athens

island holidays

Middle-class Greeks sacrifice

votes for to 128 votes against. There were 18 abstention parties forming the coalition government.



More

ON THIS STORY

'Lagarde list' journalist faces retrial Protesters disrupt Greek-German meeting

Greece's recession deepens amid austerity

Editorial Europe plays a Greek shell game

IMF and eurozone split over Greece

ON THIS TOPIC

Troika sees €2bn fiscal gap in Greek budget

Analysis Third time lucky? The latest Greek rescue

Slideshow How the latest bailout may play out

remain a member of the isolation, collapse into ba drachma". Provided parliament bac

Provided parliament bac another vote due on Sun ministers are expected to Greece's bailout loan on still have to be endorsed parliaments.

The vote was held after a measures, including cuts in pensions and public se fuel and cigarettes, and h healthcare. The retireme for recent entrants to the

8/20/13 Dutch mood shifts against austerity and the EU - FT.com FINANCIAL TIMES

August 8, 2013 5:35 pm

Dutch mood shifts against austerity and the EU

By Matt Steinglass in The Hague



The Netherlands' parliament is empty for the summer recess, but on Thursday the country's powerful labour unions staged at its doors a noisy rally, featuring angry workers, an accordion band and a wall of shoes.

> r represented the "walk a mile in our shoes" campaign the unions ed in an attempt to block C6bn in austerity measures the is planning for 2014 to be unveiled by early September. Those cuts o keep the Netherlands' budget deficit under the 3 per cent limit y EU rules, but it is not clear whether the government can push h.

Irks a slow but significant shift, as this prosperous Calvinist country, d to austerity, has gradually turned against it. The Dutch ; the strongest advocates of tough European budget deficit rules and m the start of the euro crisis in 2010. Now that the EU is forcing deficits, public support for Europe in this once strongly prolunged.



Shielded from the midday glare under a blue-and-white striped umbrella, Giorgos Priftis glances around a small beach an hour's drive from Athens which is jammed with picnicking families.

"Everyone here is in the same situation as we are - they can't afford to go away for a holiday," says the 46-year-old local government worker on his annual leave.



His wife Anna, busy unpacking a cold box, adds: "Last year we spent a week in a self-catering apartment on an island... This year I lost my job and that means we can't even eat at the beach café."

in Antonis Samaras, the cer deputies were voting on remain a member of the

Economic Policy Definition of Debt Sustainability

Sustainability rules out any of the following situations:

✓ a debt restructuring is already needed

It the borrower accumulates debt at a rate faster than the growth in its capacity to service debt

It the borrower lives beyond its means by accumulating debt in the knowledge that a major retrenchment will be needed to service these debts RECAP

Intertemporal solvency condition is weaker than the economic policy definition of sustainability

We call debt **sustainable** if a country or a government is able to service its debts without the need for implausibly large policy adjustments; renegotiating the terms of debt; or simply defaulting.

Part 1 Unit 2: Lecture 3

Debt Burden Indicators for Solvency and Liquidity: Commonly Used Ratios OUTLINE

 The concept of liquidity
 Debt burden indicators and their role
 Key solvency indicators

Key liquidity indicators



We define an entity as **liquid** if, regardless of whether it satisfies the solvency condition, its liquid assets and available financing are sufficient to meet or roll-over its maturing liabilities.

What to Watch for to Minimize Liquidity Risks

The projected trajectory AND the level of debt should be based on realistic assumptions

Risk factors include

- Market perception of the sovereign
- Debt maturity structure
- ✓ The currency composition of debt
- ✓ The availability of liquid assets

The creditor base (notably, the share of nonresident creditors)
Insolvency vs. Illiquidity

Sometimes it can be difficult to distinguish between insolvency and illiquidity situations

- Liquidity problems are often symptoms of underlying solvency problems: creditors refuse to roll over maturing debt because of solvency concerns
- Liquidity problems may give rise to insolvency, by raising interest rates or pressuring the exchange rate

Vulnerability

When we talk about debt sustainability,

vulnerability is defined as a risk that the liquidity or solvency conditions are violated and the borrower enters a crisis

How Do We Assess the Debt Burden?

By examining the projected evolution of a set of debt burden indicators over time

What are the indicators?

Debt Burden Indicators

✓ Ratios of the <u>debt stock</u> or <u>debt service</u> relative to what we define as measures of the ability to service debt (*repayment capacity*), e.g.

GDP

export proceeds

fiscal revenue

🟓 Other

✓ Gross financing needs, either in level or scaled by the above measures

Debt Burden Indicators as Measures of Solvency and Liquidity

Ratios of debt <u>stock</u> relative to repayment capacity are indicators of solvency

Ratios of <u>debt</u> service are indicators of potential liquidity problems

Gross financing needs is an indicator of potential liquidity problems

Definitions of Gross Financing Needs

✓ Gross financing needs are the amount of financing necessary to cover the deficit plus amortization of debt

GFN = Deficit + Amortization

GFN = Primary Deficit + Debt Service

✓ GFN can be positive or negative

Definitions of Debt Service and Amortization

M Debt service

DS = Interest + Amortization

✓ Amortization = principal payments coming due on medium – and long – term debt plus short – term debt coming due (maturity of 1 year or less)

Illustration: debt/GDP vs. debt/exports

Debt Ratios for an Open Economy (exports/GDP=60%) Debt Ratios for a Closed Economy (exports/GDP=10%)



Both countries have the same debt/GDP ratio, but very different debt/exports ratio.

Illustration: Gross Financing Needs and Other Debt Burden Indicators

	STD=10% total	STD=60% total
	debt	debt
	(bill I	LCU)
Gross Financing Needs (deficit plus amortization)	360	906
Deficit		
Primary deficit	22	22
Interest payments	108	108
Amortization Payments		
Short-term debt	121	728
Medium and long-term debt	109	49
Debt service (interest plus amortization)	338	884
	(%)	
Gross financing needs-to-GDP	18%	44%
Gross financing needs-to-Revenue	73%	184%
Debt service-to-GDP	17%	43%
Debt service-to-Revenue	69%	180%
Total public debt-to-GDP	66%	66%
Total public debt-to-Revenue	273%	273%

RECAP

Concept of Liquidity
 Debt Burden Indicators:
 Repayment Capacity (the ability to service debt).

Solvency and Liquidity

Part 1 Unit 2: Lecture 4

Scope of Debt Sustainability Analysis

OUTLINE

 ✓ Scope of the IMF/World Bank Debt Sustainability Analysis (DSA)
 ✓ DSA for Different Types of Debt

DSA and DSF

A DSA is produced for a particular country

- ✓ The Debt Sustainability Framework (DSF) is the framework within which DSAs are produced.
- ✓ The DSF is needed to ensure comparability across DSAs produced for different countries.

MAC DSA

For advanced and emerging economies with access to financial markets, we use the Framework for Fiscal Policy and Public Debt Sustainability Analysis in Market– Access Countries (MAC DSA)

MAC DSA (www.imf.org)

Jan Int	ernotional	What's New Site Map Site Index Contact Us Glossary		
CO M	onetary Fund	Search		
CARY V LVL	sheary rana			
Home	About the IMF Rese	arch Country Info News Videos Data and Statistics		
Publications				
	Debt Sustainability Analysis— Introduction Guidance Note on	Debt Sustainability Analysis for Market- Access Countries Last Updated: May 22, 2013 The Fund's approach to debt sustainability analysis differentiate		
	Access Countries	between market-access countries, that typically have significant access to international capital markets, and low-income countries, which meet their external financings needs mostly through concessional resources. The assessments of public and external debt sustainability are conducted in the context of both IMF program design and reviews, and Article IV surveillance. The assessments are performed through standardized templates. The <u>framework for public debt sustainability analysis</u> was reformed in 2011 and guidance to staff on the implementation of the <u>new</u> <u>framework</u> was introduced in May 2013.		
	Related Factsheets			
	IMF Surveillance			
	<u>Vulnerability</u> Indicators			
	DSA Templates			
	MAC DSA Templates: <u>External Debt</u> Public Debt	The assessment of external debt sustainability continues to be anchored by the framework introduced in June 2002 (see " <u>Assessing Sustainability</u> "). This framework was subsequently		
	(forthcoming)	Assessments-Review of Application and Methodological <u>Refinements</u> " and <u>Information Note On Modifications To The Fund's</u> <u>Debt Sustainability Assessment Framework For Market-Access</u> <u>Countries</u>).		



LIC DSF

The DSF originated as the framework to assess debt sustainability in low– income countries (LICs)

LIC DSF (www.imf.org)

Español = Français

FACTSHEET

Full text 🔎

The Joint World Bank–IMF Debt Sustainability Framework for Low-Income Countries

September 30, 2013

Low-income countries have often struggled with large external debts. Debt burdens have been reduced, thanks in large part to international debt relief initiatives. As part of the Millennium Development Goals (MDGs), the IMF and the World Bank have developed a framework to help guide countries and donors in mobilizing the financing of low-income countries' development needs, while reducing the chances of an excessive build-up of debt in the future. The joint World Bank–International Monetary Fund (IMF) Debt Sustainability Framework (DSF) was introduced in April 2005, and is periodically reviewed, to address this challenge. The most recent review was discussed by the Executive Boards of the International Development Association and the IMF in February 2012.



Public and publicly guaranteed (PPG) external debt

Public domestic debt

Public DSA

Private external debt (non-guaranteed)

Sample DSA (www.imf.org)

	INTERNATIONAL MONETARY FUND	CYPRUS121818
	CYPRUS	
December 6, 2013	SECOND REVIEW UNDER THE EXTENDED ARRANGEMENT UNDER THE EXTENDED FUND FACILITY AND REQUEST FOR 4. Balance of Payments, 2008-20	39 40 41 42
	5. External Financing Requirements and Sources, 2012-20 6. Monetary Survey, 2008-20	43
	7. Indicators of Fund Credit, 2012-20 8. Schedule of Reviews and Purchases	45 46 47
	10. Selected Reforms—Measures Completed	48 49
	12. MEFP Commitments for the Fiscal Sector	50
	1. Public Sector Debt Sustainability Analysis 2. External Sector Debt Sustainability Analysis	51 60

Scope of Public DSA

The public DSA (also called the fiscal DSA) covers total debt of the public sector, to external and domestic creditors

MAC DSA for public debt covers only public debt, not publicly guaranteed debt (PPG)

LIC DSA for public debt covers public and publicly guaranteed debt (PPG)

Scope of External DSA

The external DSA covers external debt in the economy

MAC DSA for external debt covers debt owed by <u>both</u> the public sector and the private sector

LIC DSA for external debt covers public and publicly guaranteed (PPG) external debt

Selected Features of DSA

✓ To inform a judgment on debt sustainability, the DSA for MAC and LIC combine

the indicators of solvency and liquidity
 the trajectory and the level of debt and financing needs under a baseline scenario
 the adverse scenarios recognizing the uncertainty and macro-fiscal risks, e.g.
 economic cycle (boom-bust) analysis shocks to contingent liabilities, growth, interest rate, exchange rate, etc.

Selected Features of MAC DSA

M DSA MACs for public debt considers

The market perception of the sovereign

Risks stemming from the debt profile Creditor base Maturity

Currency composition
The realism of the underlying assumptions

Selected Features of LIC DSA

✓ LIC DSA considers

a long-term prospective

the concessionality of debt

risk rating: an explicit assessment of the risk of external debt distress RECAP

 Scope of Debt Sustainability Analysis (DSA)
 MAC or LIC
 DSA for Different Types of Debt
 Public or External

Part 1 Unit 3:

Why is Debt Sustainability Analysis Important?

Understanding the costs of high debt

Learn the definition and origin of debt and other crises

✓ Understanding the mechanism of debt crisis OUTLINE

 Costs Associated with High Debt
 Types of Economic Crisis
 Mechanism of Debt Crisis

Part 1 Unit 3: Lecture 1

Costs Associated with High Debt

UNIT OUTLINE Consequences of High Debt Vulnerability to Sudden Stops Crowding out of private investment Loss of policy flexibility Debt Overhang Debt Restructuring

Consequences of High Debt

For both <u>public</u> debt and total <u>external</u> debt:

Vulnerability to a sudden stop in financing (official or private flows)

Impact of Sudden Stops

✓ External debt:

- current and capital account restrictions
- currency crisis, banking crisis, recession, default

M Public debt

drastic reduction in primary spending
 currency crisis, banking crisis, recession,
 default

Consequences of High Debt

For <u>public</u> debt, consequences include

Migher interest rates and crowding out of private investment

Less flexibility to conduct countercyclical policy

M Debt overhang

Debt Overhang

✓ Definition: The expected tax burden to finance debt is so high that it is a disincentive to current investment/consumption and hence a drag on the economic activity

✓ Consequences:

Iower growth, Iower government revenues
 insufficient funds for primary expenditures
 higher chance of default



Consequences of Sovereign Debt Restructuring

Political and economic penalties

- ✓ Spillovers across segments of the economy (especially if banks are major holders of government debt)
- Contagion to other countries
- ✓ The 1998 Russian sovereign default and fears in 2010 of a possible Greek default are examples of strong contagion to other countries
RECAP

 Costs Associated with High Debt:
 Vulnerability
 Crowding out
 Loss of flexibility

- Debt Overhang
- Debt Restructuring

Part 1 Unit 3: Lecture 2

Types of Economic Crises

OUTLINE

Types of Economic Crises
 Currency Crises
 Banking Crises
 External Debt Crises
 Sovereign Debt Crises

Currency Crises

What: an attack in a country's currency results in one, or a combination, of the following

large devaluation
sharp depreciation
large increase in interest rates
large fall in reserves

✓ When: concerns about the viability of the exchange rate regime or the level of the exchange rate

Currency Crises

✓ Why:

market expects that foreign exchange (FX) reserves will run out because of inconsistent policies or be insufficient to cover short-term debt

market expects government to devalue in order to address a policy goal, such as improved competitiveness

Banking Crises

✓ What: run on banks or large-scale government intervention to rescue banks

When: concerns about solvency and liquidity of banks

Banking Crises

- M Why:
 - bursting bubble in equity or real estate prices
 - interest rate, exchange rate, or
 growth shocks

bust typically follows lending booms (stimulated by financial liberalization/capital inflows)

Debt Crises

Debt crises can be associated with either sovereign (public) or commercial (private) debt

Sovereign Debt Crises

✓ What: defaults, involuntary restructuring of sovereign debt, or belief that this is about to occur

When: often combined (or immediately following) banking crises:

this was true for over 60 percent of all sovereign debt crises after 1970 (Rogoff and Reinhart, 2010)

Sovereign Debt Crises

✓ Why:

financial rescue packages extended period of low growth fiscal profligacy (including war finance) failed state-owned enterprises

natural disasters



External Debt Crises

✓ What: payment arrears on a substantial fraction of external debt

✓ When: cash flow problems or difficulties obtaining foreign exchange

M Why:

"sudden stops" following capital inflow episode

interest rate, exchange rate, or growth shocks

RECAP

✓ Different Types of Economic Crises:

Currency Crises

Banking Crises

External Debt Crises

Sovereign Debt Crises



Please watch the video on Latvia :

Debt and BoP crisis with internal devaluation and fiscal adjustment

Part 1 Unit 3: Lecture 3

Mechanism of Sovereign Debt Crises

✓ Sample Mechanism of Debt Crisis

✓ Bank-sovereign Interdependence A Sample Mechanism of a Sovereign Debt Crisis

Financial sector rescue packages weigh on public debt and the deficit

Economic activity nosedives

 Fiscal revenue collapses while expenditures skyrocket

A Sample Mechanism of a Sovereign Debt Crisis

The resulting spike in deficits and debt causes concerns about the fiscal balance and debt sustainability

Costs of borrowing for the sovereign increase

Fiscal position further worsens

Bank-Sovereign Interdependence

✓ Damage to bank balance sheets→bailout costs and increase in sovereign debt

✓ Increase in sovereign debt→higher possibility of sovereign default, lower ratings→damage to bank balance sheets

Bank-Sovereign Interdependence



RECAP

Sample mechanism of debt crisis

M Bank-sovereign Interdependence

Part 1 Unit 4

Public Debt Sustainability in a Closed Economy

LIND

Learn how to derive the law of motion for public debt

Learn how to derive the formal solvency condition for public debt

<u>Closed economy</u>:

debt

Law of motion for public debt
 Solvency condition for public

Part 1 Unit 4: Lecture 1

Law of Motion for Public Debt

OUTLINE

The debt-deficit relationship
 The primary balance
 The government budget constraint

The Relationship between Deficit and Public Debt

Current Stock of Debt = Past Stock of Debt

+ Deficit

+ Other Flows

+ Exchange Rate Valuation

✓ In the closed economy, we assume debt is issued in local currency, so that there is no contribution of exchange rate valuation. In the open economy, we allow for debt issued in local currency and in foreign currency.

Vicious Circle of Debt and Deficit



Relationship between Deficit and Public Debt

- Budget deficit can be financed by <u>borrowing</u> or other means (e.g., printing money or selling assets)
- Net new borrowing necessary to finance budget deficit adds to the current stock of debt

PUBLIC DEBT DYNAMICS CLOSED ECONOMY

NOTATION

stock of debt

PB,

i,

 $D_{+} = D_{++1} + \Delta D_{+}$

interest spending

government revenues

government primary (non-interest) spending

primary or (non-interest) surplus $PB_{+} = R_{+} - G_{+}$

 $I_{\dagger}=i_{\dagger}D_{\dagger-1}$

nominal interest rate

- real interest rate r,
- inflation rate Π,
- $P_{+}Y_{+}$ nominal GDP real GDP growth rate g,

 $(1+i_{+}) = (1+\pi_{+})(1+r_{+})$

 $P_{+}Y_{+} = (1+\pi_{+})(1+g_{+})P_{+}Y_{+}$

FLOW BUDGET CONSTRAINT

$$G_{+} + i_{+}D_{+-1} - R_{+} + OT_{+} = (D_{+} - D_{+-1})$$

$$Other flows,$$
e.g. bank
recapitalization Change
Revenues in debt

Note

Other flows include

✓ asset purchases and expenditure items not included in G

- bank recapitalization
- assumption of guaranteed state enterprise debt
- ✓ non-debt sources of financing
 - asset sales such as privatization revenues
 - seigniorage

Such non-debt sources of financing enter with a negative sign

Focusing on Primary Balance:

✓ Substitute the primary balance definition:

 $-PB_{t} + i_{t}D_{t-1} + OT_{t} = D_{t} - D_{t-1}$

 \checkmark Assume other flows are zero: $OT_t = 0$

Equation for Debt Dynamics:

$D_t = (1 + i_t) D_{t-1} - PB_t$

Example: Evolution of Debt over Time



Part 1 Unit 4: Lecture 2

Deriving the Solvency Condition
OUTLINE

✓ Deriving the Solvency Condition from the Flow Budget Constraint:

 Derive the Intertemporal Budget Constraint

Impose Transversality

Obtain Solvency Condition

Checkpoint: Where Are We?

We talked about the debt-deficit relationship

We derived the government budget constraint

We derived one-period law of motion for public debt

Checkpoint: what's next?

- We will start with the flow budget constraint
- We will use forward substitution to derive the intertemporal budget constraint
- Which we need to obtain solvency condition (in present-value terms)

FLOW BUDGET CONSTRAINT

 $D_{t} = (1+i_{t})D_{t-1}PB_{t}$

INTERTEMPORAL BUDGET CONSTRAINT FOR T=2

$$D_{1} = (1+i) D_{0} - PB_{1}$$

$$D_{2} = (1+i) D_{1} - PB_{2}$$

$$= (1+i)((1+i) D_{0} - PB_{1}) - PB_{2}$$

$$= D_{1}$$

$$D_{2} = (1+i)^{2} D_{0} - (1+i) PB_{1} - PB_{2}$$

INTERTEMPORAL BUDGET CONSTRAINT FOR T=N

-!-

$D_{N} = (1+i)^{N} D_{0} - \sum_{j=1}^{N} (1+i)^{N-j} PB_{j}$

DERIVING SOLVENCY CONDITION

By dividing both sides by $(1+i)^{\mathbb{N}}$ and putting D_0 on the other side, we have the following expression:

$$D_{o} = \sum_{j=1}^{N} \left(\frac{1}{1+i}\right)^{j} PB_{j} + \left(\frac{1}{1+i}\right)^{N} D_{N}$$

TRANSVERSALITY (NO-PONZI SCHEME) CONDITION

 $\lim_{N \to \infty} \left(\frac{1}{1+i}\right)^N D_N = 0$

Meaning of Transversality Condition: it prohibits issuing more and more debt without ever repaying principal and interest on the previously accumulated stocks.

SOLVENCY CONDITION

Solvency: Assuming transversality (no-Ponzi scheme), the outstanding initial debt should be covered by the present value of future primary balances:

$$D_0 = \sum_{j=1}^{\infty} \left(\frac{1}{1+i}\right)^j PB_j$$

Part 1 Unit 5

Public Debt Sustainability In Closed Economy: Part 2

UNIT m

Learn how to derive the law of motion for the ratio of public debt-to-GDP for a closed economy

Analyze contributions of key macroeconomic variables to debt dynamics

Obtain the debt-stabilizing
 primary balance

<u>Closed economy:</u>

Law of motion for public-debtto GDP ratio

M Automatic debt dynamics

✓ Debt-stabilizing primary balance

Part 1 Unit 5: Lecture 1

Law of Motion for Public Debt-to-GDP in a Closed Economy

OUTLINE

Law of motion for public-debtto GDP ratio

Key macroeconomic variables affect debt sustainability

Primary balance
 Initial level of debt
 Growth

Real interest rate

Checkpoint: Where Are We?

We are still in the case of a closed economy (to avoid worrying about the exchange rate-induced variations in debt)

Checkpoint: what's next?

We are about to get pragmatic and do some derivations in terms of ratios of debt stock to the economy's capacity (GDP)

Law-of-motion for debt-to-GDP in hand, we will look at the impact of the key macroeconomic variables on debt dynamics

LAW OF MOTION: THE DEBT-TO-GDP RATIO

Evolution of government debt at time t $D_{+} = (1+i_{+}) D_{+-1} - PB_{+}$ (1)

By dividing (1) by nominal GDP, P,Y,

$$\frac{D_{t}}{P_{t}Y_{t}} = \frac{(1+i_{t})}{(1+\pi_{t})(1+g_{t})} \frac{D_{t-1}}{P_{t-1}Y_{t-1}} - \frac{PB_{t}}{P_{t}Y_{t}}$$
$$\frac{D_{t}}{P_{t}Y_{t}} = \frac{PB_{t}}{P_{t}Y_{t}}$$

DYNAMICS OF DEBT-TO-GDP RATIO

Evolution of the debt-to-GDP ratio using the definition of the real interest rate

- | -

$$\phi_{+} = \frac{(1+r_{+})}{(1+g_{+})} d_{+-1} - pb_{+} (2)$$

$$\phi_{+} = \frac{(1+r_{+})}{(1+r_{+})} = \frac{(1+r_{+})}{(1+g_{+})}$$

$$\frac{f(t)}{f(t)} = \frac{f(t)}{f(t)} + \frac{f(t)}{f(t)$$

LAW-OF-MOTION FOR THE DEBT-TO-GDP RATIO

Evolution of the debt-to-GDP ratio

$$d_{t} = \left(\frac{(1+r_{t})}{(1+g_{t})}\right) d_{t-1} - pb_{t}$$
(2)

A higher primary balance $\rightarrow \rightarrow \rightarrow$ a lower debt/GDP ratio A higher initial debt $\rightarrow \rightarrow \rightarrow$ a higher debt/GDP ratio A higher growth rate $\rightarrow \rightarrow \rightarrow$ a lower debt/GDP ratio A higher real interest rate $\rightarrow \rightarrow \rightarrow$ a higher debt/GDP ratio

Part 1 Unit 5: Lecture 2

Stabilizing Debt in a Closed Economy

OUTLINE

Automatic debt dynamics
 Stability of debt
 Debt stabilizing primary balance

M The danger of debt momentum

AUTOMATIC DEBT DYNAMICS

We can distinguish favorable from unfavorable automatic debt dynamics:

$$d_{+} - d_{+-1} = \left(\frac{r_{+} - g_{+}}{1 + g_{+}} \right) d_{+-1} - pb_{+} (2)$$
Automatic
debt dynamics

- r < g: favorable debt dynamics
- r > g: unfavorable debt dynamics





Primary Balance to Stabilize Debt:

Assuming d is constant one can solve for the debt stabilizing primary balance pb*:



Automatic debt dynamics

Primary Balance to Stabilize Debt:

The primary surplus needed to keep the debt/GDP constant equals the debt dynamics. It is proportionate to the gap between real interest rate and real growth rate

The primary balance needed to keep the debt/GDP constant will rise directly with the size of the initial debt/GDP, if r>g

We can also interpret the equation as telling us the level of debt which can be sustained for a given primary balance

The Danger of Debt Momentum:

The primary surplus needed to keep the debt/GDP constant will rise directly with the size of the initial debt/GDP

The higher is the initial debt stock, the more difficult it is to stabilize the debt/GDP ratio

✓ Danger of built in momentum, the higher debt-to-GDP ratio gets, the less likely it is to run a sufficiently large primary surplus debt rises

✓ Thus, vulnerability rises with debt-to-GDP ratio

Illustration: Evolution of Debt/GDP over Time:

 $d_{t} = \frac{(1+r_{t})}{(1+g_{t})} d_{t-1} - pb_{t}$





 Law of motion for public-debtto GDP ratio
 Automatic debt dynamics
 Debt-stabilizing primary balance

Part 1 Unit 6

Public Debt Sustainability In Open Economy

UNIT m

Learn how to derive the law of motion for public debt for an open economy

Obtain the debt-stabilizing
 primary balance

Analyze contributions of key macroeconomic variables to debt dynamics OUTLINE

<u>Open economy:</u>

Law of motion for public debt

✓ Debt-stabilizing primary balance

M Comparative statics

Part 1 Unit 6: Lecture 1

Law of Motion for Public Debt in an Open Economy

OUTLINE

✓ Flow budget constraint with external financing

✓ Law of motion for the debt-to-GDP ratio

M Automatic debt dynamics

43 PUBLIC DEBT DYNAMICS OPEN ECONOMY
NOTATION

 $\begin{array}{c} D^{D}_{+} \\ D^{F}_{-} \\ i_{+} \\ i_{+} \\ i_{+} \\ e_{+} \\ e_{+} \\ e_{+} \\ \alpha_{+} \end{array}$

stock of domestic currency denominated debt (domestic debt) stock of foreign currency denominated debt (foreign debt) nominal interest rate on domestic debt nominal interest rate on foreign debt effective nominal interest rate nominal exchange rate (domestic currency per \$) rate of exchange rate depreciation share of foreign currency denominated debt

GOVERNMENT BUDGET CONSTRAINT

Now suppose the government can borrow from abroad as well as domestically.



Domestic currency denominated debt

Foreign currency (\$) denominated debt

Nominal exchange rate (local currency per \$)

FLOW BUDGET CONSTRAINT

The flow budget constraint becomes:

63

$$D_{t}^{d} + e_{t}D_{t}^{f} = (1+i_{t}^{d})D_{t-1}^{d} + (1+i_{t}^{f})e_{t}D_{t-1}^{f} - PB_{t} + OT_{t}$$
(1)

FLOW BUDGET CONSTRAINT

This can be re-expressed as:

$$D_{+} = (1+i_{+}^{a})(1-\alpha_{+1})D_{+1} + (1+i_{+}^{f})\alpha_{+1}(1+\epsilon_{+})D_{+1} - PB_{+} + OT_{+1}$$

where we introduced the share of foreign currency denominated debt α and ϵ is the rate of exchange rate depreciation

$$\alpha_{t-1} = e_{t-1} D_{t-1}^{f} / D_{t-1}$$

DEBT DYNAMICS WITH EXTERNAL FINANCING

-;-

Dividing both sides by GDP at date t:

$$d_{t} = \frac{\left[1+i_{t}^{w} + \alpha_{t-1} \epsilon_{t}(1+i_{t}^{f})\right]}{(1+g_{t})(1+\pi_{t})} d_{t-1} - pb_{t} + ot_{t} (2)$$

i^w weighted average of domestic and foreign nominal interest rates
 i^f nominal interest rates in foreign-currency denominated debt
 change in the exchange rate (local currency per U.S. dollar)
 α share of foreign-currency denominated public debt

DEBT LAW OF MOTION: LINKING TO THE REAL INTEREST RATE

Another way of expressing the debt-law-of motion:

-1-

$$d_{t} = \underbrace{(1+r_{t}^{d})}_{(1+g_{t})} d_{t-1}^{d} + \frac{(1+i_{t}^{f})(1+\varepsilon_{t})}{(1+g_{t})(1+\pi_{t})} d_{t-1}^{f} - pb_{t} + ot_{t}$$

$$(2')$$

$$(1+r_{t}^{d}) = \frac{(1+i_{t}^{d})}{(1+\pi_{t})}$$

$$\frac{CHANGE IN DEBT TO GDP RATIO}{d_{t} = \phi_{t}^{*} d_{t-1} - pb_{t} + ot_{t}}$$

Subtract d_{t-1} on both sides:
$$\Delta d_{t} = (\phi_{t}^{*} - 1)d_{t-1} - pb_{t} + ot_{t} \quad (3)$$

Automatic debt dynamics

COEFFICIENT ON AUTOMATIC DEBT DYNAMICS:

-¦-

$$\phi_{+}^{*} - 1 = \frac{i_{+}^{w} - \pi_{+}(1 + g_{+}) - g_{+} + \alpha_{+-1} \varepsilon_{+}(1 + i_{+}^{f})}{(1 + g_{+})(1 + \pi_{+})}$$
(3)

AUTOMATIC DEBT DYNAMICS:

$$d_{t}-d_{t-1} = \frac{i_{t}^{w} - \pi_{t}(1+g_{t})}{(1+g_{t})(1+\pi_{t})}d_{t-1} - \frac{g_{t}}{(1+g_{t})(1+\pi_{t})}d_{t-1} + \frac{\varepsilon_{t}\alpha_{t-1}(1+i_{t}^{f})}{(1+g_{t})(1+\pi_{t})}d_{t-1} - pb_{t}+ot_{t}$$

Contribution of the effective real interest rate

Contribution of the real GDP growth

Contribution of exchange rate depreciation

Part 1 Unit 6: Lecture 2

Stabilizing Debt in an Open Economy

OUTLINE

Debt stabilizing primary balance

Comparative statics: role of key macroeconomic variables:

Initial level of debt

🛹 Growth

Interest Rate

🛹 Exchange Rate

-:--

$$\Delta d_{+} = (\phi_{+}^{*} - 1) d_{+-1} - pb_{+} + ot_{+} (3)$$
$$d_{+} = d_{+-1}$$

$$pb_{+}^{*} = (\phi_{+}^{*} - 1)d_{+} + ot_{+}$$

$$\frac{\text{DEBT-STABILIZING PRIMARY BALANCE}}{\text{pb}^{*} = \frac{(r_{t}^{w} - g_{t}) + \alpha_{t-1} \varepsilon_{t}^{*} (1 + r_{t}^{f})}{(1 + g_{t})} \quad d_{t-1} + ot_{t}$$
Automatic debt dynamics
$$r^{w} = \alpha r^{f} + (1 - \alpha) r^{d} \qquad (1 + \varepsilon^{*}) = \frac{(1 + \varepsilon) (1 + \pi^{*})}{(1 + \pi)}$$

Key Comparative Statics:

- ✓ The required primary balance is higher when:
 - The real interest rate growth differential is large
 - Other flows contribute to an increase in debt (e.g. financial sector support measures, nationalization of private pensions)
 - There is exchange rate depreciation (ε) in countries with large foreign exchange denominated debt (α)
- Note: The last two are examples of "stock-flow adjustments" because they help reconcile the change in the value of debt with the deficit

Illustration:

Key Macro-Economic Variables

	Country W	Country X	Country Y	Country Z
		(% change)		
r ^d	5	4	5	5
r ^f				5
•				5
g	4	5	4	4
٤*	0	0	0	5
		(% GDP)		
d ^d	100	100	20	50
d ^f	0	0	0	50
pb*	0.96	-0.95	0.19	3.49

Illustration:

We can calculate pb* by applying the formula, while being careful to express interest rates and growth rates as a percent:

$$pb^{*} = \frac{(r_{t}^{w} - g_{t})d + \varepsilon^{*}(1 + r_{t}^{f})d^{f}}{(1 + g_{t})}$$

✓ For country Z for example:

 $pb^* = \frac{(0.05 - 0.04) \bullet 1 + 0.05 \bullet (1 + 0.05) \bullet 0.5}{(1 + 0.04)} = 0.0349 = 3.49\%$



✓ Debt Law-of-Motion M Debt-stabilizing Primary Balance

✓ Key Comparative Statics

Part 1 Unit 7

Chipping Away at Public Debt

LIND

✓ Understand different adjustment paths and their implications

✓ Understand how fiscal adjustment may affect GDP and the risk premium on government debt OUTLINE

✓ Adjustment Paths and Their Implications

> Front-loaded and back-loaded adjustments

 Fiscal Adjustment, the Business Cycle, and the Risk Premium

✓ History of Past Fiscal Adjustments (video)

Part 1 Unit 7: Lecture 1

Adjustment Paths and Their Implications

OUTLINE

M Definition of front-loaded and back-loaded adjustment

M Circumstances favoring each

Front-loaded and Back-loaded Adjustment:

Front-loaded adjustment:



M Back-loaded adjustment:



Front-loaded and Back-loaded Adjustment:

Front-loaded fiscal adjustment quickly raises the primary balance to the "targeted" level

M Back-loaded adjustment phases in the adjustment over time

Circumstances Affecting the Timing of Adjustment: Front-loading may be necessary: when facing severe financing constraints >to build credibility to seize opportunity of political support M Back-loading may be preferable to: support to economic activity ensure quality of measures

Circumstances Affecting the Timing of Adjustment:

Credibility is very important in the context of high debt, because of its effect on the risk premium and therefore debt dynamics

✓ In the case of back-loading, credibility can be enhanced by institutional mechanisms, such as balanced budget rules and procedural rules

Circumstances Affecting the Timing of Adjustment:

If fiscal adjustment has a negative impact on growth, it may undermine debt sustainability

undertake fiscal adjustment in the upswing of the business cycle

 undertake fiscal adjustment during worldwide recoveries

support fiscal adjustment with accommodating monetary policy

Front-loaded and Back-loaded Adjustment

In the Additional Resources we provide a formula for the fiscal adjustment necessary to reduce debt over a given number of periods. The formula allows one to distinguish frontloaded adjustment from back-loaded adjustment.

REDUCING DEBT IN & PERIODS

First, we define the future debt target as a proportion of the actual debt:

$$d_{t+k}^* = \gamma^* d_t$$
 with $\gamma^* \leq 1$

Assuming a constant interest rate, GDP growth rate, and government primary balance (pb*) we can express the solvency condition as:

$$d_{\dagger} = \left(\frac{1}{\phi}\right)^{k} \gamma^{*} d_{\dagger} + pb^{*} \sum_{j=1}^{k} \left(\frac{1}{\phi}\right)^{j}$$

USEFUL FORMULA FOR GEOMETRIC SERIES

$$\sum_{j=1}^{k} ar^{j} = a \left(\frac{r - r^{k+1}}{1 - r} \right)$$

REDUCING DEBT IN & PERIODS

The needed primary balance (pb*) to reduce the debt from d to d* in k periods corresponds to:

$$pb^{*} = \left(\frac{(\phi - 1)(\gamma^{*} - \phi^{k})}{1 - \phi^{k}}\right)d_{t}$$

The lower γ^{\star} and/or k, the larger pb^ would need to be to reach the debt target in the desired time



✓ This material took stock of:

 The primary balance necessary to reduce debt to certain level
 the potential impact on cost of funding RECAP

✓ The tradeoff between frontloaded and back-loaded fiscal adjustment is

front-loading to ease financing constraints and gain credibility

VS.

back-loading to support growth and work out quality measures

Part 1 Unit 7: Lecture 2

Fiscal adjustment and the business cycle

✓ How the budget balance affects GDP

Mow the budget balance affects the risk premium

Fiscal Adjustment and the Business Cycle


Fiscal Adjustment and the Business Cycle

Three main channels from primary balance to debt/GDP:

 directly via the primary balance in the debt dynamics

via GDP through demand

lower government spending and higher taxes reduce demand

via interest rates through credibility (risk premium) and demand

crowding out

Fiscal Adjustment and the Business Cycle

- Fiscal consolidation may lead to slower GDP growth
 - High multiplier (closed economy, high unemployment)
 - Coordinated consolidations in economic partners
- Fiscal consolidation may lead to lower interest rates
 - In high-debt countries credibility effects are particularly important



Front-loaded vs back-loaded adjustment

✓ The speed at which debt can be reduced depends on how fiscal adjustment affects GDP and interest rates.

Additional Resources

Please watch the video on Chipping Away At Public Debt

Part 1 Unit 8

Role of Macroeconomic Policies

LIND

✓ Understand the role of monetary policy

✓ Understand the economic policy tradeoffs

OUTLINE

Monetary Policy Stance and Debt Molicy Tradeoffs

Part 1 Unit 8: Lecture 1

Monetary Policy Stance and Debt

OUTLINE

✓ Expansionary monetary policy—possible effects

The effect of monetary policy on interest rates and inflation

✓ Interest rate

M Inflation

M Exchange rate

M Growth

Expansionary monetary policy possible effects

Lower nominal interest rates

Lower real interest rates

Higher inflationHigher growth

Depreciated exchange rate

✓ Use the debt dynamics equation and assuming at first no foreign currency debt:

if real interest rates fall and growth improves (therefore improving the primary balance), debt is reduced.

$$d_{t} \downarrow = \frac{(1+r_{t} \downarrow)}{(1+g_{t})} d_{t-1} - (pb_{t} \uparrow + ot_{t})$$

✓ If there is foreign currency debt, the effect is no longer unambiguous. Debt/GDP could increase, in the case of less than complete pass-through of exchange rate depreciation to inflation.

$$d_{t} = \frac{(1+r_{t}^{d})}{(1+g_{t}^{d})} d_{t-1}^{d} + \frac{(1+i_{t}^{f})(1+\varepsilon_{t})}{(1+g_{t})(1+\tau_{t}^{d})} d_{t-1}^{f} - (pb_{t}^{\uparrow}+ot_{t})$$

Illustration: Impact of Monetary Easing

 $d_t \approx (r_t^d - g_t)d_{t-1}^d + (i_t^f + \varepsilon_t - g_t - \pi_t)d_{t-1}^f - pb_t - ot_t$

	Easing of monetary policy			
			Depreciation	
		No change in	Passthrough	Passthrough
	No easing	exchange rate	20%	100%
		(% change)		
r ^d	6	4	4	4
i ^f	3	3	3	3
٤*	0	0	10	10
π	0	0	2	10
g	3	4	5	4
pb	-2	-1.5	-1	-1.5
		(% GDP)		
d ^d _{t-1}	50	50	50	50
d ^f _{t-1}	50	50	50	50
dt	105.0	103.0	106.1	103.0

✓ The effect of monetary policy on interest rates and inflation needs to be qualified

Expansionary monetary policy tends to reduce short-term interest rates but increase long-term ones, reflecting expectations of future inflation

M Fischer equation: $i=r^*+\pi^e$

- ✓ Interest rates are set based on a required real return r*
 - Given r*, higher πe translates into higher i
 - Ex post r need not equal r* if there is surprise inflation (in which case r<r*)</p>

Part 1 Unit 8: Lecture 2

Policy Tradeoffs

OUTLINE

 Sustainable Debt vs. Inflation
 Sustainable Debt vs. Competitiveness

🗹 Sustainable Debt vs. Fairness

Policy Tradeoffs

M Fiscal dominance

✓ Fear of floating

✓ Fairness/income distribution

Policy Tradeoffs: Sustainable Debt vs. Inflation

- Fiscal dominance: inability to conduct contractionary monetary policy because it would jeopardize government debt dynamics
- Contractionary monetary policy, which would result in
 - higher real interest rates
 - lower growth

higher debt/GDP

Policy Tradeoffs: Sustainable Debt vs. Competitiveness

✓ <u>Fear of Floating</u>: reluctance to allow a floating exchange rate to depreciate

Loose monetary policy is helpful for competitiveness and growth, but will raise the value of foreign currency debt expressed in local currency (public and private) and may cause bankruptcies

Policy Tradeoffs: Sustainable Debt vs. Competitiveness

Fear of floating follows from the "original sin"—the inability of emerging markets to issue external debt in their own currency.

Policy Tradeoffs: Sustainable Debt vs. Fairness

✓ Inflation as default

There is a thin line separating inflation from default since inflation erodes away the value of debt (especially when there is "financial repression" capping nominal interest rates)

Inflation creates a redistribution of wealth from creditors to debtors

Part 1 Unit 9

External Debt Sustainability

UNIT

Understanding similarities between external and fiscal sustainability

✓ Understanding external debt creating flows

✓ Understanding solvency condition for external debt OUTLINE

M External DSA

- ✓ External debt creating flows
- ✓ Debt law-of-motion
- ✓ Solvency condition for external debt

Part 1 Unit 9: Lecture 1

External Debt Creating Flows

OUTLINE

✓ External DSA

External debt creating flows

✓ The adjusted balance

External DSA:

- ✓ Similarities between external and fiscal sustainability → apply similar methodologies
- Focus on external debt of the country (including the private sector debt)
- ✓ The current account balance of the balance of payments takes the place of the overall budget balance.

Key Differences with Public Debt:

The government does not directly control the CAB

- ✓ In a healthy cycle, exports and CAB will improve over time, allowing for repayment of debt
- Exchange rate normally plays larger
 role in external sustainability

External Debt Creating Flows:

• Our goal in this unit is to derive a law of motion for external debt, which links debt to past debt and the current account balance.

$$D_t^f = (1 + i_t^f) D_{t-1}^f - AB_t$$

✓ In the process we will define the adjusted balance, AB, which is a modified current account balance.

Notation:

 CA_t current account balance AB_t adjusted balance interest payments on external debt l_t KAt capital account FA+ financial account A_t external assets Lt external liabilities D_t^f external debt liabilities external equity liabilities E_t $(P_{+}Y_{+})$ GDP expressed in USD = $P_{+}Y_{+}/e_{+}$

All variables are expressed in USD

The Adjusted Balance:

✓ Define:

 $AB_t = (CA_t + I_t) + (\Delta E_t - \Delta A_t)$

non-interest current account balance non-debt financing

✓ The current account (the sum of net exports, income and current transfers) records interest payments on debt as a negative income item. Here we add interest back to obtain the noninterest CAB.

Part 1 Unit 9: Lecture 2

External Financing Constraint and Debt-Lawof-Motion

П	
	Ζ
	Ī
\mathbf{F}	
	\mathbf{C}
C	2

✓ External Financing Constraint✓ Debt Law-of-motion

External Financing Constraint

✓ Using the terminology of the BOP and IIP manual (6th edition), we write:

 $CA_t + KA_t = FA_t$

✓ We assume for simplicity that the capital account KA (capital transfers for the most part) is zero.

$$KA_t = 0$$
External Financing Constraint

✓ The financial account of the BOP records the acquisition of assets and the incurrence of liabilities (e.g. as the result of external borrowing). These flows are called "transactions".

We assume for simplicity that valuation effects are zero, so that the change in the value of assets and liabilities is equal to these BOP transactions. $CA_{t} = \Delta A_{t} - \Delta L_{t}$

FA,

External Financing Constraint

Liabilities can be either debt liabilities or equity liabilities:

$$CA_{t} = \Delta A_{t} - (\Delta D_{t}^{f} + \Delta E_{t})$$
$$\Delta L_{t}$$

✓ Debt includes debt securities, loans, currency and bank deposits. Equity includes shares and foreign direct investment.

Debt Law-of-motion

Rewriting the previous equation in terms of current period debt and adding and deducting interest:

$$D_{t}^{f} = D_{t-1}^{f} - CA_{t} - \Delta E_{t} + \Delta A_{t} - I_{t} + I_{t}$$
$$-AB_{t}$$

More Next assume as before: $I_t = i_t^f D_{t-1}^f$

Debt Law-of-motion

Finally, using the definition of the adjusted balance and grouping terms involving lagged debt, we find the law-of-motion we had set out to find:

$$D_t^f = (1 + i_t^f) D_{t-1}^f - AB_t$$

Part 1 Unit 9 Lecture 3:

Solvency condition for external debt

Solvency condition for external debt

From the debt law-of-motion we can obtain the intertemporal budget constraint through repeated substitution, as we did for public debt.

✓ We then obtain the solvency condition for external debt by imposing the tranversality condition or No-Ponzi condition. Specifically, we require that the present discounted value of external debt at time infinity approaches zero.

Solvency Condition For External Debt

✓ Using a the same method as for public debt, the intertemporal budget condition extended to N periods is:

$$D_0^f = \sum_{j=1}^N \left(\frac{1}{1+i_t^f}\right)^j AB_j + \left(\frac{1}{1+i_t^f}\right)^N D_N^f$$

✓ We extend this formula to time infinity and impose the transversality condition.

Solvency Condition

Solvency: the present value of all surpluses (of the adjusted balance) is equal to initial debt.

$$D_0^f = \sum_{j=1}^{\infty} \left(\frac{1}{1+i_t^f}\right)^j AB_j$$

RECAP

 External Debt Sustainability Analysis
 External Debt Creating Flows
 Debt Law-of-motion
 Solvency condition for external debt

Part 1 Unit 10 Lecture 1:

Deriving External Debt Law-of-Motion

OUTLINE

✓ Debt Law-of-motion: The Debt-To-GDP Ratio

M Automatic Debt Dynamics

External Debt Law-of-Motion: the Debt-to-GDP Ratio

✓ Evolution of external debt at time t:

$$D_t^f = (1 + i_t^f) D_{t-1}^f - AB_t$$

✓ We divide by GDP expressed in USD, (P_tY_t)*, since external debt is expressed in USD.

$$\frac{D_{t}^{f}}{(P_{t}Y_{t})^{*}} = \frac{(1+i_{t}^{f})D_{t-1}^{f}}{(1+g_{t})(1+\pi_{t})P_{t-1}Y_{t-1}/e_{t}} - \frac{AB_{t}}{(P_{t}Y_{t})^{*}}$$

$$P_{t}Y_{t}$$

Debt Law-of-Motion: the Debt-To-GDP Ratio

✓ We convert GDP in local currency back to GDP in USD and use $1+\varepsilon_t=e_t/e_{t-1}$



Debt Law-of-Motion: the Debt-to-GDP Ratio

It is easy to show that

$$\frac{(1+i_t^f)(1+\varepsilon_t)}{(1+\pi_t)} = (1+r_t^f)(1+\varepsilon_t^*)$$

where

$$(1+r_t^f) = \frac{(1+i_t^f)}{(1+\pi^*)} \qquad (1+\varepsilon^*) = \frac{(1+\varepsilon)(1+\pi^*)}{(1+\pi)}$$

 π^* = foreign inflation rate r_t^f = real interest rate on foreign debt ϵ^* = real exchange rate depreciation

Debt Law-of-Motion: Analytical Representation

Evolution of the debt-to-GDP ratio Φ_t

 $d_{t}^{f} = \underbrace{\frac{(1+r_{t}^{f})(1+\varepsilon^{*}_{t})}{(1+g_{t})}}_{(1+g_{t})} d_{t-1}^{f} - ab_{t}$

For $ab_t = 0$ and $d_{t-1} > 0$:

If $\phi_t < 1$, debt converges to zero If $\phi_t > 1$, debt explodes

Automatic Debt Dynamics

✓ Deducting past debt from both sides and simplifying:

$$d_{t}^{f} - d_{t-1}^{f} = \frac{(1 + r_{t}^{f})(1 + \varepsilon_{t}^{*})}{(1 + g_{t})} d_{t-1}^{f} - d_{t-1}^{f} - ab_{t}$$

automatic debt dynamics
$$d_{t}^{f} - d_{t-1}^{f} = \underbrace{\frac{r_{t}^{f} - g_{t} + \varepsilon_{t} * (1 + r_{t}^{f})}{(1 + g_{t})}}_{(1 + g_{t})} d_{t-1}^{f} - ab_{t}$$

Debt-Stabilizing Adjusted Balance

What level of ab keeps debt constant? To find the answer, simply set $d_t=d_{t-1}$ in the previous expression (denote the constant debt level by d^*) $ab^* = \frac{r_t^f - g_t + \varepsilon^* (1 + r_t^f)}{(1 + g_t)} d^*$

✓ ab* is the <u>debt-stabilizing primary surplus</u>. Note that it equals the automatic debt dynamics.

If ab>ab* debt falls continuously; if ab<ab*, debt explodes and is therefore unsustainable

Key Comparative Statics

M Debt dynamics are affected by: Real interest rate Growth rate of the economy Current level of indebtedness Net exports Long-term level of other flows Real exchange rate changes

Illustration

	Country X	Country Y	Country Z	
		(% change)		•
r	5	5	5	
g	4	4	4	
3	0	0	-2	
		(% GDP)		
ď	100	20	100	
ab*	~~~			~~~

Illustration

✓ We can calculate ab* by applying the formula, <u>while being careful</u> to divide the parameters by 100:

$$ab^{*} = \frac{r_{t}^{f} - g_{t} + \varepsilon^{*} (1 + r_{t}^{f})}{(1 + g_{t})} d^{*}$$

✓ For country Z for example:

$$ab^* = \frac{0.05 - 0.04 - 0.02(1 + 0.05)}{(1 + 0.04)} \bullet 1 = -0.0106 = -1.06\%$$

Summary

Key Takeaways for External Debt

Key Equations

Debt law-of-motion

 $D_{t}^{f} = (1 + i_{t}^{f})D_{t-1}^{f} - AB_{t}$

Adjusted balance

 $AB_t = (CA_t + I_t) + (\Delta E_t - \Delta A_t)$

Debt law-of-motion (%GDP)

 $d_{t}^{f} - d_{t-1}^{f} = \frac{r_{t}^{f} - g_{t} + \varepsilon_{t}^{*}(1 + r_{t}^{f})}{(1 + g_{t})} d_{t-1}^{f} - ab_{t}$

Debt dynamics

M Debt dynamics are affected by: Real interest rate Growth rate of the economy Current level of indebtedness Net exports Long-term level of other flows Real exchange rate changes